$\bar{\mathbf{K}}$ -nucleus dynamics: from quasibound states to kaon condensation

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Abstract Coupled-channel $\bar{K}N$ dynamics near threshold and its repercussions in few-body \bar{K} -nuclear systems are briefly reviewed, highlighting studies of a K^- pp quasibound state. In heavier nuclei, the extension of mean-field calculations to multi- \bar{K} nuclear and hypernuclear quasibound states is discussed. It is concluded that strangeness in finite self-bound systems is realized through hyperons, with no room for kaon condensation.

Key words KN dynamics, K-nuclear quasibound states, kaon condensation

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1 Introduction

The gross features of low-energy $\bar{K}N$ physics are encapsulated in the leading-order Tomozawa-Weinberg (TW) vector term of the chiral effective Lagrangian [1]. The Born approximation for the \bar{K} -nuclear optical potential $V_{\bar{K}}$ due to the TW interaction term yields then a sizable attraction:

$$V_{\bar{K}} = -\frac{3}{8f_{\pi}^2} \rho \sim -55 \frac{\rho}{\rho_0} \text{ MeV}$$
 (1)

for $\rho_0 = 0.16 \text{ fm}^{-3}$, where $f_\pi \sim 93 \text{ MeV}$ is the pseudoscalar meson decay constant. Iterating the TW term plus the less significant NLO terms, within an in-medium coupled-channel approach constrained by the $\bar{K}N-\pi\Sigma-\pi\Lambda$ data near the $\bar{K}N$ threshold, roughly doubles this K-nucleus attraction. A major uncertainty in these chirally based studies arises from fitting the $\Lambda(1405)$ resonance by the imaginary part of the $\pi\Sigma(I=0)$ amplitude calculated within the same coupled channels chiral scheme. However, irrespective of this uncertainty, the $\Lambda(1405)$ which may be viewed as a K⁻p quasibound state quickly dissolves in the nuclear medium at low density, so that the repulsive free-space scattering length a_{K^-p} , as function of ρ , becomes attractive well below ρ_0 . Adding the weakly density dependent I = 1 attractive scattering length $a_{K^{-}n}$, the resulting in-medium KN isoscalar scattering length $b_0(\rho) = \frac{1}{2}(a_{K^-p}(\rho) + a_{K^-n}(\rho))$ translates into a strongly attractive $V_{\bar{K}}$:

$$\operatorname{Re}V_{\bar{K}}(\rho_0) = -\frac{2\pi}{\mu_{KN}} \operatorname{Re}b_0(\rho_0)\rho_0 \sim -110 \text{ MeV}.$$
 (2)

The underlying K⁻p forward scattering amplitude is shown in Fig. 1.

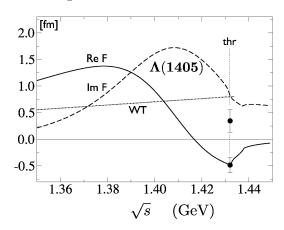


Fig. 1. The K⁻p forward scattering amplitude calculated in the chiral SU(3) coupled channel approach [2]. The scattering length deduced from the DEAR kaonic hydrogen measurement [3] is also shown. The dotted, almost horizontal line indicates the TW amplitude. Figure adapted from Ref. [4].

Comprehensive fits to the strong-interaction shifts and widths of K^- -atom levels provide phenomenological evidence for a strongly attractive, and also strongly absorptive \bar{K} -nucleus interaction near

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threshold [5, 6]. These fits yield extremely deep density dependent optical potentials with nuclear-matter depth $-\text{Re} V_{\bar{K}}(\rho_0) \sim (150 - 200) \text{ MeV}$ at threshold. Fig. 2 illustrates the real part of the best-fit K-nucleus potential for ⁵⁸Ni as obtained for several models. The corresponding values of χ^2 for 65 K⁻-atom data points are given in parentheses. A model-independent Fourier-Bessel (FB) fit [7] is also shown, within an error band. Just three terms in the FB series, added to a $t\rho$ potential, suffice to achieve a χ^2 as low as 84 and to make the potential extremely deep, in agreement with the density-dependent best-fit potentials DD and F. In particular, potential F provides by far the best fit ever reported for any global K⁻-atom data fit [8], and the lowest χ^2 value as reached by the FB method.

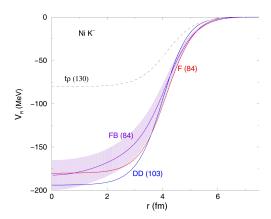


Fig. 2. (color online). Real part of the $\bar{K}-^{58}Ni$ potential for several density dependent potentials (DD, FB, F) and a $t\rho$ potential fitted to kaonic-atom data [6]. χ^2 values are given in parentheses.

In Fig. 3 I show the overlap of the 4f atomic radial wavefunction squared with the matter density $\rho_{\rm m}$ in ⁵⁸Ni for two of the models exhibited in Fig. 2. The 4f atomic orbit is the last circular K^- atomic orbit from which the K⁻ meson undergoes nuclear absorption. The figure demonstrates that, whereas this overlap for the shallower $t\rho$ potential peaks at nuclear density of order 10% of ρ_0 , it peaks at about 60% of ρ_0 for the deeper DD potential and has a secondary peak well inside the nucleus. The double-peak structure indicates the existence of a K⁻ strong-interaction $\ell = 3$ quasibound state for the DD potential. It is clear that whereas within the $t\rho$ potential there is no sensitivity to the interior of the nucleus, the opposite holds for the density dependent F potential which accesses regions of full nuclear density. This owes partly to the smaller imaginary part of F.

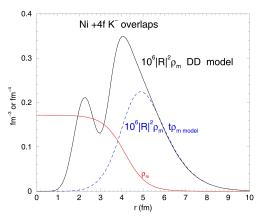


Fig. 3. (color online). Overlaps of K⁻ 4f atomic radial wavefunctions R squared with $\rho_{\rm m}$ of 58 Ni, for the $t\rho$ and DD fits of Fig. 2. The nuclear matter density $\rho_{\rm m}$ is shown for comparison. Figure provided by Eli Friedman.

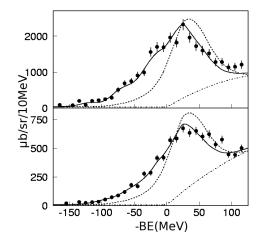


Fig. 4. KEK-PS E548 missing mass (K^-,n) (upper) & (K^-,p) (lower) spectra on $^{12}{\rm C}$ at $p_{\rm K^-}=1~{\rm GeV}/c$ [9].

A fairly new and independent evidence in favor of extremely deep K-nucleus potentials is provided by (K^-,n) and (K^-,p) spectra taken at KEK on ¹²C [9] and very recently also on ¹⁶O (presented in PANIC08) at $p_{K^-} = 1 \text{ GeV}/c$. The ¹²C spectra are shown in Fig. 4, where the solid lines represent calculations (outlined in Ref. [10]) using potential depths in the range 160-190 MeV. The dashed lines correspond to using relatively shallow potentials of depth about 60 MeV which may be considered excluded by these data. However, Magas et al. have recently expressed concerns about protons of reactions other than those directly emanating in the (K⁻,p) reaction and which could explain part of the bound-state region of the measured spectrum without invoking a very deep \bar{K} nuclear potential [11]. A sufficiently deep potential would allow quasibound states bound by over 100 MeV, for which the major $\bar{K}N \to \pi\Sigma$ decay channel is blocked, resulting in relatively narrow \bar{K} -nuclear states. Of course, a fairly sizable extrapolation is involved in this case using an energy-independent potential determined largely near threshold.

A third class, of shallower potentials with $\text{Re}V_{\bar{K}}(\rho_0) \sim -(40\text{--}60)$ MeV, was obtained by imposing a Watson-like self-consistency requirement on the nuclear-medium $\bar{K}N$ $t(\rho)$ matrix that enters the optical potential $V_{\bar{K}} = t(\rho)\rho$ [12, 13]. This is due to the suppressive effect of $\text{Im}t(\rho)$ in the K⁻ propagator of the Lippmann-Schwinger equation for $t(\rho)$:

$$t(\rho) = v + v \frac{1}{E - H_{\text{mB}}^{(0)} - t(\rho)\rho - V_{\text{N}} + i0} t . \tag{3}$$

Here v and $t(\rho)$ are coupled-channel meson-baryon (mB) potential and in-medium t matrix, respectively, and $H^{(0)}$ is the kinetic energy operator which depends implicitly on the density ρ through the imposition of the Pauli principle in $\bar{\rm KN}$ intermediate states. The K⁻ optical potential $t(\rho)\rho$ and the nucleon potential $V_{\rm N}$ act only in $\bar{\rm KN}$ intermediate states. A sizable ${\rm Im} t(\rho)$ leads to exponential decay of the propagator $(E-H_{\rm mB}^{(0)}-t(\rho)\rho-V_{\rm N}+{\rm i}0)^{-1}$, so that $t(\rho)\approx v$ thus losing the cooperative coupling effect to the $\pi {\rm Y}$ channels in higher-order terms of v. However, one needs then to worry about higher orders in the chiral expansion which are not yet in.

I start this review by making brief remarks on the $\bar{K}N-\pi\Sigma$ system, followed by reviewing topics related to \bar{K} nuclear quasibound states: (i) the K^- pp system as a prototype of few-nucleon quasibound states of \bar{K} mesons; and (ii) multi- \bar{K} nucleus quasibound states.

$2 \quad \overline{K}N - \pi\Sigma$ coupled channels

Modern chirally motivated $\bar{K}N - \pi\Sigma$ coupledchannel models give rise to two Gamow poles that dominate low-energy KN dynamics. Representative pole positions are shown in Fig. 5 and their model dependence is demonstrated in Fig. 6. The $\Lambda(1405)$ resonance, studied in final-state $\pi\Sigma$ interactions, is determined in these models primarily by the lower pole. This identification is further supported, as shown in Fig. 7, by the trajectory of the lower pole which merges into a genuinely I=0 bound state below the $\pi\Sigma$ threshold when the KN interaction is sufficiently increased. The upper pole appears in this chiral model [16] above the KN threshold. Its position and the trajectory it follows away from the real energy axis make it largely model dependent and sensitive to off-shell effects.

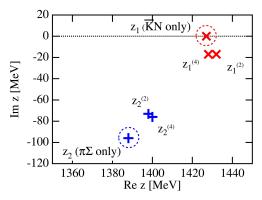


Fig. 5. (color online). Pole positions in the complex energy (z) plane of the $\bar{K}N$ (I=0) scattering amplitude resulting from single-channel, two-channel and full (four-channel) models [14].

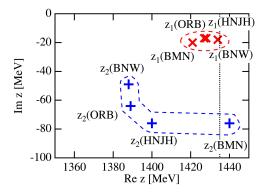


Fig. 6. (color online). Poles of the $\bar{\rm KN}$ (I=0) scattering amplitude in several chiral model applications listed in Ref. [14]. The dotted vertical line denotes the $\bar{\rm KN}$ threshold.

KN coupling scaled

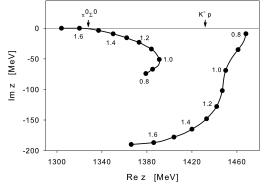


Fig. 7. Trajectories of Gamow poles in the complex energy (z) plane, on the Riemann sheet $[\Im k_{\bar{K}N}, \Im k_{\pi\Sigma}] = [+,-]$, upon scaling the $\bar{K}N$ interaction strengths [15]. The $\pi^0\Sigma^0$ and K^-p thresholds are marked by arrows.

Surprisingly, however, it is the upper two-body pole that is found to affect significantly three-body $[\bar{\mathrm{K}}(\mathrm{NN})_{I=1} - \pi \Sigma \mathrm{N}]_{I=1/2}$ coupled channel calculations for the K⁻pp system. The trajectory of the only Gamow pole in this system that qualifies for representing a quasibound state is depicted in circles in Fig. 8. Similarly to the trajectory of the $\Lambda(1405)$ in the two-body case, this quasibound $\bar{\mathrm{K}}\mathrm{NN}$ pole also merges into a genuinely bound state below the $\pi \Sigma \mathrm{N}$ threshold which becomes, upon extending the model space, a quasibound $\pi \Sigma \mathrm{N}$ state decaying to the $\pi \Lambda \mathrm{N}$ and YN lower channels ignored here.

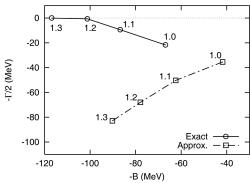


Fig. 8. Variation of $\bar{\text{KNN}}(I=1/2)$ quasibound state energy with $\bar{\text{KN}}$ interaction strength in three-body coupled-channel (circles) and single-channel (squares) calculations [17].

3 Few-nucleon $\bar{\mathbf{K}}$ systems

The lightest K nuclear configuration maximizing the strongly attractive I = 0 KN interaction is $[K(NN)_{I=1}]_{I=1/2,J^{\pi}=0^{-}}$, loosely denoted as K⁻pp. The FINUDA collaboration presented evidence in K⁻ stopped reactions on several nuclear targets for the process $K^-pp \to \Lambda p$, interpreting the observed signal as due to a K-pp deeply bound state with $(B,\Gamma) \approx (115,67) \text{ MeV } [18].$ However, this interpretation has been challenged in Refs. [8, 19]. A new analysis of DISTO pp \rightarrow K⁺ Λ p data claims a K⁻pp signal with $(B,\Gamma) \approx (103,118)$ MeV [20], see Fig. 9. Its location practically on top of the $\pi\Sigma N$ threshold, and particularly the large width, are at odds with any of the few-body calculations listed below, posing a problem for a K⁻pp quasibound state interpretation.

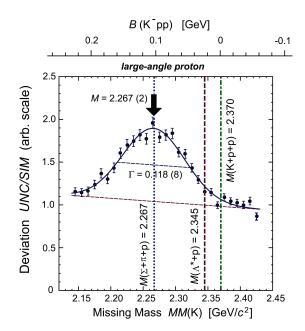


Fig. 9. (color online). K^+ missing-mass spectrum in the reaction pp $\to K^+\Lambda p$ measured at $T_p=2.85$ GeV by the DISTO collaboration [20]. The peak structure with a background (thin line) gives $M=2267\pm 2,~\Gamma=118\pm 8$ MeV.

Results of few-body calculations for the K⁻pp system are displayed in Table 1. The marked difference between the 'K̄NN single channel' binding energies $B_{\rm K^-pp}$ reflects the difference between the input K̄N amplitudes: the YA I=0 single-pole amplitude [21] resonates at 1405 MeV, whereas the DHW I=0 amplitude [23] resonates at 1420 MeV (close to the upper of two poles). This dependence on the input amplitudes has been verified in a recent coupled-channel Faddeev study [27] and in the variational calculations of Ref. [26].

A notable feature of the K⁻pp coupled-channel calculations [24–26] in Table 1 is that the explicit use of the $\pi\Sigma N$ channel adds about 20 ± 5 MeV to the binding energy calculated using effective $\bar{K}N$ potential within a single-channel calculation. This is demonstrated in Fig. 8 by comparing corresponding points on the two trajectories shown there.

Table 1. Calculated K⁻pp binding energies (B_{K^-pp}) , mesonic (Γ_m) & nonmesonic (Γ_{nm}) widths (in MeV).

	K̄NN single channel		$\bar{K}NN - \pi \Sigma N$ coupled channels		
	variational [21, 22]	variational [23]	Faddeev [24]	Faddeev [25]	variational [26]
$B_{\mathrm{K^-pp}}$	48	17-23	50-70	60–95	40-80
$\Gamma_{ m m}$	61	40-70	90-110	45 - 80	40-85
$\Gamma_{ m nm}$	12	4–12			~ 20

Besides present $p(p, K^+)$ measurements [28] at GSI, improving on the DISTO $pp \to K^+\Lambda p$ data, the K^-pp system will be explored at J-PARC in the ${}^3\text{He}(K^-,n)$ and $d(\pi^+,K^+)$ reactions [29].

4 Multi- \bar{K} nucleus quasibound states from RMF calculations

Dynamical relativistic mean field (RMF) calculations of single-K quasibound states yield separation energies in the range 100-150 MeV for potentials compatible with K⁻ atom data [30]. By scanning on the ω vector-field and σ scalar-field strengths, these calculations also provide a quantitative estimate of the width $\Gamma_{\rm K^-}$ as a function of the K⁻ separation energy B_{K^-} . The width comes out larger than 100 MeV near threshold, decreasing to 50 MeV or slightly more as soon as the primary $\bar{K}N \to \pi\Sigma$ decay mode shuts off 100 MeV below threshold [30, 31]. A full systematics for ¹²C is shown in Fig. 10 which also demonstrates the substantial gain in B_{K^-} and Γ_{K^-} for $B_{\rm K^-} > 100$ MeV when the nuclear core is allowed to adjust dynamically in response to the additional mean field generated by the K meson. It is worth noting that the resulting nuclear central densities do not increase by more than a factor 2 with respect to ρ_0 , and even that is limited to a region of 1–2 fm about the origin. The figure also shows that ${\rm Im}V_{ar{{
m K}}}$

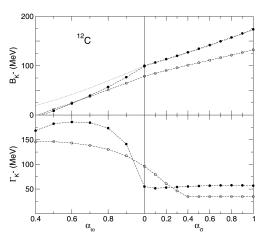


Fig. 10. 1s K⁻ separation energy $B_{\rm K^-}$ and width $\Gamma_{\rm K^-}$ in $^{12}{\rm C}$, calculated statically (open circles) and dynamically (solid circles) as a function of the ω KK and σ KK fractional coupling strengths α_{ω} and α_{σ} , respectively, with α_{ω} varied in the left panels as indicated while $\alpha_{\sigma}=0$, and with α_{σ} varied in the right panels as indicated while holding $\alpha_{\omega}=1$. The dotted line shows $B_{\rm K^-}$ when Im $V_{\bar{\rm K}}$ is switched off in the dynamical RMF calculation [30].

may safely be ignored in the calculation of separation energies near and above 100 MeV. These results for $B_{\rm K^-}$ and $\Gamma_{\rm K^-}$, and for nuclear densities, were shown in the RMF calculations of Mareš et al. [30] and Gazda et al. [31] to hold over a comprehensive range of nuclei from $^{12}{\rm C}$ to $^{208}{\rm Pb}$.

Highlights of multi- \bar{K} nuclear calculations are summarized below, based on recent work by Gazda et al. [32, 33]. In order to establish correspondence with chiral models, particularly with the leading-order TW term, the \bar{K} coupling constants to the vector meson fields were chosen to obey F-type SU(3) symmetry, namely $\alpha_{\rm V} \equiv F/(F+D)=1$:

$$2g_{\omega KK} = \sqrt{2} g_{\phi KK} = 2 g_{\rho KK} = g_{\rho \pi \pi} = 6.04,$$
 (4)

where the value of $g_{\rho\pi\pi}$ is due to the $\rho \to 2\pi$ decay width. The value of $g_{\omega \text{KK}}^{SU(3)} = 3.02$ is lower than any of the other choices made in previous works, as detailed in Ref. [32]. The $\bar{\text{K}}$ coupling constant to the scalar field σ , $g_{\sigma \text{KK}}$, was used to fit prescribed values of B_{K^-} in nuclear systems with a single $\bar{\text{K}}$ meson. The resulting values of $g_{\sigma \text{KK}}$ are also lower than those commonly used, e.g. those inspired by quark models.

 K_{1s}^- separation energies B_{K^-} in multi- K^- nuclei $^{40}\mathrm{Ca} + \kappa K^-$ are shown in Fig. 11 for two choices of $g_{\sigma KK}$, designed within each RMF model to produce $B_{K^-} = 100$ and 130 MeV for $\kappa = 1$. The difference between the various curves, for a given starting value of B_{K^-} , originates from the specific balance in each one of these RMF models between the vector fields and the scalar field. A robust saturation of B_{K^-} with κ is observed, independently of the applied RMF model, owing to the isoscalar vectormeson fields (ω, ϕ) which induce repulsion between like \bar{K} mesons. Additional repulsion, in this particular case, is caused by the isovector vector-meson field ρ .

The saturation values of B_{K^-} in Fig. 11 are considerably lower than what would be required to convert Λ hyperons to \bar{K} mesons through strong decays $\Lambda \to p + K^-$, and also $\Xi^- \to \Lambda + K^-$, in multi-strange hypernuclei which hence remain the lowest-energy configuration for multi-strange systems [34]. This is demonstrated in Fig. 12 for various multi-strange hypernuclei constructed under realistic assumptions on the meson-field couplings to Λ and Ξ hyperons [33]. The figure shows little dependence of B_{K^-} on whether or not Ξ hyperons are added to Λ hyperons (in a ²⁰⁸Pb core) and very little dependence (in a ⁹⁰Zr core) on the potential depth assumed for Ξ hyperons in nuclei $(V_{\Xi}^{R} = -25 \text{ MeV} \text{ as opposed to the unmarked})$ $V_{\Xi}^{\rm R} = -18$ MeV that corresponds relativistically to the nonrelativistic value $V_{\Xi}^{NR} = -14 \text{ MeV}$ determined

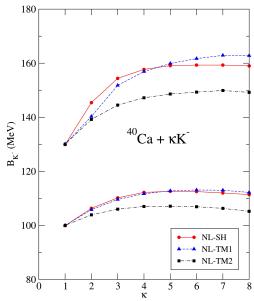


Fig. 11. (color online). K⁻ separation energy $B_{\rm K^-}$, calculated in several nuclear RMF models (see inset) for multi-K⁻ nuclei 40 Ca+ κ K $_{1s}^-$. The lower (upper) group of curves was constrained to produce $B_{\rm K^-}=100$ (130) MeV for $\kappa=1$ [32].

in the BNL-E885 experiment [35]). These RMF calculations across the periodic table provide a powerful argument against \bar{K} condensation under strong-interaction equilibrium conditions in terrestial experimentation. It does not apply, however, to kaon condensation in neutron stars, where equilibrium config-

urations are determined by weak-interaction conditions.

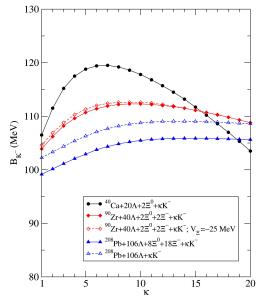


Fig. 12. (color online). RMF calculations of multi- \bar{K} quasibound states as a function of the number κ of \bar{K} mesons in multi-strange nuclei [33].

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