# Study of Exclusive Hadronic Decays for $D^0 \rightarrow K_s^0 \pi^+ \pi^-$ and $D^0 \rightarrow K_s^0 K^+ K^-$ and Their Resonant Structures \*

#### **BES** Collaboration

BAI Jing-Zhi BAN Yong<sup>5</sup> BIAN Jian-Guo CAI Xiao CHANG Jin-Fan CHEN He-Sheng CHEN Hong-Fang<sup>1</sup> CHEN Jiang-Chuan CHEN Jie<sup>8</sup> CHEN Yuan-Bo CHI Shao-Peng CHU Yuan-Ping CUI Xiang-Zong DAI You-Shan<sup>3</sup> DAI Yu-Mei<sup>12</sup> DONG Liao-Yuan DU Shu-Xian<sup>10</sup> DU Zhi-Zhen FANG Jian FANG Shuang-Shi FU Cheng-Dong FU Hong-Yu FU Li-Ping<sup>11</sup> GAO Cui-Shan GAO Mei-Li GAO Yuan-Ning<sup>14</sup> GONG Wen-Xuan GU Shu-Di GUO Ya-Nan, GUO Yi-Qing GUO Zi-Jin<sup>7</sup> HAN Shi-Wen HE Ju HE Kang-Lin HE Mao<sup>2</sup> HE Xiang HENG Yue-Kun HONG Tao HU Hai-Ming HU Tao HUANG Guang-Shun HUANG Liang<sup>11</sup> HUANG Xiu-Ping JI Xiao-Bin JIANG Chun-Hua JIANG Xiao-Shan JIN Da-Peng JIN Shan JIN Yan KE Zun-Jian LAI Yuan-Fen LI Fei LI Gang LI Hui-Hong<sup>6</sup> LI Jia-Cai LI Jin LI Kan<sup>11</sup> Ren-Ying LI Ru-Bo LI Wei LI Wei-Guo LI Xue-Qian<sup>8</sup> LI Xue-Song<sup>14</sup> LIU Chao-Feng<sup>10</sup> LIU Chun-Xiu LIU Feng<sup>6</sup> LIU Huai-Min LIU Jian-Bei LIU Jue-Ping<sup>10</sup> LIU Rong-Guang LIU Yan LIU Zhen-An LIU Zhong-Xiu LU Gong-Ru<sup>2</sup> LÜ Feng LÜ Hai-Jiang<sup>1</sup> LÜ Jun-Guang LÜ Zhi-Jian LUO Xiao-Lan MA En-Cheng MA Feng-Cai<sup>12</sup> MA Ji-Mao MAO Ze-Pu MENG Xiang-Cheng MO Xiao-Hu' NIE Jing NIE Zhen-Dong PENG Hai-Ping<sup>1</sup> QI Na-Ding QIAN Cheng-De<sup>4</sup> QIU Jin-Fa RONG Gang<sup>1)</sup> SHEN Ding-Li SHEN Hong SHEN Xiao-Yan SHENG Hua-Yi SHI Feng SONG Li-Wen SUN Han-Sheng SUN Sheng-Sen<sup>1</sup> SUN Yong-Zhao SUN Zhi-Jia TANG Su-Qiu TANG Xiao TIAN Ding TIAN Yu-Run<sup>14</sup> TONG Guo-Liang WANG Jin-Zhu WANG Jun WANG Lan WANG Ling-Shu WANG Man WANG Meng WANG Pei-Liang WANG Ping WANG Wen-Feng WANG Yi-Fang WANG Zhe WANG Zheng WANG Zhi-Yong<sup>7</sup> WEI Cheng-Lin WU Ning XIA Xiao-Mi XIE Xiao-Xi XU Guo-Fa XU Ye XUE Sheng-Tian YAN Mu-Lin<sup>1</sup> YAN Wen-Biao YANG Gui-An YANG Hong-Xun<sup>14</sup> YANG Jie<sup>1</sup> YANG Sheng-Dong YE Ming-Han<sup>7</sup> YE Yun-Xiu<sup>1</sup> YING Jun<sup>5</sup> YU Chuan-Song YU Guo-Wei YUAN Chang-Zheng YUAN Jian-Ming YUAN Ye YUE Qian ZANG Shi-Lei ZENG Yun<sup>11</sup> ZHANG Bing-Xin ZHANG Bing-Yun ZHANG Chang-Chun ZHANG Da-Hua ZHANG Jia-Wen ZHANG Jian ZHANG Jun-Mei<sup>9</sup> ZHANG Liang-Sheng ZHANG Qin-Jian ZHANG Shao-Qiang ZHANG Xue-Yao<sup>2</sup> ZHANG Yi-Yun<sup>13</sup> ZHANG Yong-Jun<sup>5</sup> ZHANG Yue-Yuan ZHANG Zi-Ping<sup>1</sup> Hong-Yu ZHAO Di-Xin ZHAO Jia-Wei<sup>1</sup> ZHAO Jing-Wei ZHAO Ping-Ping ZHAO Wei-Ren ZHAO Yu-Bin ZHAO Zheng-Guo<sup>2)</sup> ZHENG Jian-Ping ZHENG Lin-Sheng ZHENG Zhi-Peng ZHONG Xue-Chu ZHOU Bao-Qing ZHOU Gao-Ming ZHOU Li ZHOU Neng-Feng ZHU Ke-Jun ZHU Qi-Ming ZHU Ying-Chun ZHU Yong-Sheng ZHU Yu-Can ZHU Zi-An ZHUANG Bao-An ZOU Bing-Song

(Institute of High Energy Physics, CAS, Beijing 100039, China)

1 (Department of Modern Physics, University of Science and Technology of China, Hefei 230027, China)

<sup>2 (</sup>Department of Physics, Shandong University, Ji'nan 250100, China)

<sup>3 (</sup>Department of Physics, Zhejiang University, Hangzhou 310028, China)

Received 25 February 2003, Revised 11 September 2003

<sup>\*</sup> Supported by NSFC (19991480), National Natural Science Funds for Distinguished Young Scholar (10225524, 10225525), Major Subject of Chinese Academy of Sciences (KJ95T-03), 100 Talents Program of CAS (U-24, U-25), Knowledge Innovation Project of CAS (U-602, U-34)

<sup>1)</sup> E-mail: rongg@mail.ihep.ac.cn

<sup>2)</sup> Visiting professor to University of Michigan, Ann Arbor, MI48109, USA

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4 (Department of Applied Physics, Shanghai Jiaotong University, Shanghai 200030, China)
5 (Department of Technical Physics, Peking University, Beijing 100871, China)
6 (Institute of Particle Physics, Huazhong Normal University, Wuhan 430079, China)
7 (China Center for Advanced Science and Technology (CCAST), Beijing 100080, China)
8 (Department of Physics, Nankai University, Tianjin 300071, China)
9 (College of Physics and Information Engineering, Henan Normal University, Xinxiang 453002, China)
10 (College of Physics and Information Electionic, Wuhan University, Wuhan 430072, China)
11 (Department of Applied Physics, Hunan University, Changsha 410082, China)
12 (Department of Physics, Liaoning University, Shenyang 110036, China)
13 (Department of Physics, Sichuan University, Chengdu 610064, China)
14 (Department of Physics, Tsinghua University, Beijing 100084, China)
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**Abstract** We report the results of an experimental study of the exclusive hadronic decays for  $D^0 \to K_s^0 \pi^+ \pi^-$  and  $K_s^0 K^+ K^-$  and their resonant structures using BES- I detector at the BEPC Collider. Using the data sample of 22.3 pb<sup>-1</sup> collected at the center-of-mass energy  $\sqrt{s} = 4.03$  GeV, we measured the branching fraction for  $D^0 \to \overline{K}^0 \pi^+ \pi^-$  to be  $(5.32 \pm 0.53 \pm 0.40)\%$ , the branching fractions for the decays  $D^0 \to K^+ \pi^+$ ,  $D^0 \to \overline{K}^0 \rho^0$  and  $D^0 \to \overline{K}^0 (\pi^+ \pi^-)_{\text{non-resonant}}$  to be  $(6.05 \pm 0.32 \pm 0.49)\%$ ,  $(1.17 \pm 0.17 \pm 0.13)\%$  and  $(1.35 \pm 0.22 \pm 0.17)\%$ , respectively. We measured the branching fractions  $Br(D^0 \to f)$  to be  $(1.04 \pm 0.24 \pm 0.16)\%$  for  $f = \overline{K}^0 K^+ K^-$ ,  $(1.12 \pm 0.34 \pm 0.15)\%$  for  $f = \overline{K}^0 \phi$ , and  $(0.27 \pm 0.13 \pm 0.03)\%$  for  $f = \overline{K}^0 (K^+ K^-)_{\text{non-$\phi$}}$ .

Key words BES, BEPC, Do meson, branching fraction

#### 1 Introduction

It is still not yet possible to describe exclusive nonleptonic decays of the charmed hadrons for theory based on general principles. In the factorization [1] and nonfactorization effective calculations<sup>[2]</sup>, the determination of the hadronic matrix elements of the weak currents are all model dependent. To test the theoretical assumptions the measurements of some two body hadronic decay branching fractions of D mesons are important. For instance, measurements of the branching fractions for  $D^0 \rightarrow K^{*-} \pi^+$  and  $D^0 \rightarrow \overline{K}^0 \rho^0$  can help to clarify the theoretical aspects of the effective strengths  $a_1$  and  $a_2$  of color favored (see Fig. 1(a)) and suppressed (see Fig. 1(b)) amplitudes, respectively. Measurement of the branching fraction for D<sup>0</sup>  $\rightarrow \overline{K}^0 \phi$  is useful in estimation of the contributions of Wexchange diagram (see Fig. 1(c)) to D<sup>0</sup> decay. QCD potential models based on valence quarks expect that such W-exchange process are helicity and color suppressed<sup>[3]</sup>. However, emission of soft gluons in the initial state or explicit presence of gluons in the wave function may remove the helicity suppression. Some theoretical models predict that the contribution of W-exchange diagram to D<sup>0</sup> decay range from 1 % to 60 % of the total Do width [4]. Further experiment input is crucial.

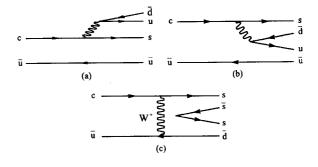


Fig.1. Decay diagram.

ARGUS<sup>[5]</sup>, MARK- $\mathbb{II}^{[6]}$ , CLEO<sup>[7]</sup> and E687<sup>[8]</sup> experiments measured the branching fractions for the decays, and some of them studied the resonant structures in the decays. In this paper we present decay branching fractions and resonant substructure measurements of  $D^0 \rightarrow K_s^0 \pi^+ \pi^-$ , and  $D^0 \rightarrow K_s^0 K^+ K^-$  with an integrated luminosity of 22.3 pb<sup>-1</sup> of data collected using BES- I detector at  $\sqrt{s} = 4.03$  GeV at BEPC  $e^+ e^-$  collider during the years 1992—1994.

#### 2 The BES- I detector

BES- I is a conventional cylindrical magnetic detector operated at the Beijing Electron Positron Collider (BEPC)<sup>[9]</sup>. A four-layer central drift chamber (CDC)

surrounding the beam pipe provides an event trigger. A forty-layer main drift chamber (MDC) located just outside the CDC provides measurements of charged tracks and ionization energy loss (dE/dx) with a solid angle coverage of 85 % of  $4\pi$  for charged tracks. Momentum resolution of 1.7 %  $\sqrt{1+p^2}$  (p in GeV/c) and dE/dx resolution of 8.5 % for Bhabha electrons are obtained for the data taken at  $\sqrt{s} = 4.03 \,\text{GeV}$ . An array of 48 scintillation counters surrounds the MDC and measures the time of flight (TOF) of charged tracks with a resolution of about 350 ps for Bhabha electrons and 450 ps for hadrons. Surrounding the TOF is a 12-radiation-length, lead-gas barrel shower counter (BSC) operated in limited streamer mode, which measures the energy of electrons and photons over 80 % of the total solid angle, with an energy resolution of  $\sigma_{\rm E}/E = 0.22/\sqrt{E} \, (E \text{ in GeV})$ , and spatial resolution of  $\sigma_{\phi} = 4.5$  mrad and  $\sigma_{z} = 2$  cm for the electrons. Outside the BSC is a solenoidal magnet providing a 0.4 T magnetic field for the central tracking region of the detector. Three double-layer muon counters instrument the magnet flux return, and serve to identify muons of momentum greater than 500 MeV/c. They cover 68 % of the total solid angle with longitudinal (transverse) spatial resolution of 5 cm (3 cm). End-cap time-of-flight and shower counters extend coverage to the forward and backward regions, but we do not use information from the end-cap counters in this analysis.

#### 3 Event selection

Events are required to contain at least four reconstructed charged tracks with good helix fits. In order to ensure good momentum resolution and charged particle identification, the tracks are required to be within  $|\cos\theta|<0.8$ , where  $\theta$  is the polar angle. All tracks, save those from  $K_s^0$  decays, must originate from the interaction region. Pions and Kaons are identified by means of TOF and  $d\it E/d\it x$  measurements. Identification requires consistency with the pion or kaon hypothesis at a confidence level greater than 1 %. In order to reduce misidentification, kaon candidates are further required to have a larger likelihood for the kaon hypothesis than for the pion hypothesis.

For the  $K_s^0$  reconstruction, we require the momentum vector of the two oppositely charged pions to be aligned with the position vector of the secondary vertex in the xy plane within 37°. The secondary vertex is required to be greater than 0.4 cm away from the collision point in xy plane, and the z coordinates of the two pion tracks to be within 5 cm of the secondary vertex. The invariant mass of  $\pi^+\pi^-$  pair is required to be within  $\pm$  13 MeV/ $c^2$  of  $K_s^0$  nominal mass.

After applying the above cuts, signals for  $D^0$  are clearly evident in the momentum spectra for the mode  $D^0 {\longrightarrow} K_s^0 \pi^+ \pi^-$  as shown in Fig.2. The lower momentum peak in the figure corresponds to D mesons from the  $D^* \, \overline{D}^*$ , and the higher momentum peak is due to  $D \, \overline{D}^*$ .

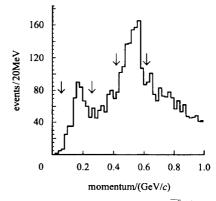


Fig. 2. Momentum distribution of  $\overline{K}^0 \pi^+ \pi^-$ .

To reduce combinatorial backgrounds in these inclusive  $D^0$  meson samples, events from which the  $K^+\,K^-\,\pi^+\,\pi^-$  or  $\pi^+\,\pi^-\,\pi^+\,\pi^-$  momentum are within the intervals from 0.06 to 0.26 or from 0.42 to 0.62 GeV/c are used to select the inclusive decays  $D^0\!\rightarrow\! K_s^0\,\pi^+\,\pi^-$  and  $D^0\!\rightarrow\! K_s^0\,K^+\,K^-$ .

#### 4 Analysis and results

#### 4.1 The decay $D^0 \rightarrow K_s^0 \pi^+ \pi^-$

## 4.1.1 The branching fraction for $D^0 \rightarrow K_s^0 \pi^+ \pi^-$

The invariant mass spectrum for the  $K_s^0\pi^+\pi^-$  combinations satisfying these selection criteria and analysis cuts described in Section 3 is shown in Fig.3. Fitting to this mass spectrum with a Gaussian function plus a 2nd order polynomial background, we obtain 755.7  $\pm$  65.0 events for the  $D^0 \rightarrow K_s^0\pi^+\pi^-$  decay after correcting to doubly

counted events. After subtracting  $K_s^0$  sideband background we obtained a number of 685.0 ± 67.1 events for the decay. The MC efficiency of reconstructing the decay  $D^0 \rightarrow \overline{K}^0 \pi^+ \pi^-$  is  $\epsilon (D^0 \rightarrow \overline{K}^0 \pi^+ \pi^-) = 0.049 \pm 0.001$ , where the error is statistical. The branching fraction for the decay  $\overline{K}^0 \rightarrow \pi^+ \pi^-$  is included in the efficiency.

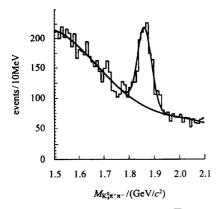


Fig. 3. Invariant mass distribution of  $\overline{K}^0\pi^+\pi^-$ .

In order to measure the relative branching ratio of  $D^0 \to \overline{K}^0 \pi^+ \pi^-$  over  $D^0 \to K^- \pi^+$ , we reconstruct the decay  $D^0 \to K^- \pi^+$  by selecting  $K^-$  and  $\pi^+$  charged tracks using the same events selection criteria as mentioned in Section 3. Fig. 4. shows the  $K^+ \pi^-$  invariant mass distribution for events for which the momenta of the  $K^- \pi^+$  combinations are within the same intervals as that used to select the inclusive decay events for  $D^0 \to K^0_s \pi^+ \pi^-$ . Fitting to this mass spectrum, we obtain 3948.3  $\pm$  95.6 events. The MC efficiency of reconstructing the  $D^0 \to K^- \pi^+$  is  $\epsilon(D^0 \to K^- \pi^+) = (0.394 \pm 0.007)$ . Using these numbers and efficiencies we obtain the relative branching ratio of  $D^0 \to \overline{K}^0 \pi^+ \pi^-$  over  $D^0 \to K^- \pi^+$  to be

$$\frac{Br(D^0 \to \overline{K}^0 \pi^+ \pi^-)}{Br(D^0 \to \overline{K}^- \pi^+)} = 1.40 \pm 0.14 \pm 0.10,$$

where the first error is statistical and the second systematic. The systematic error is estimated based on changes in the ratio due to the uncertainties in the number of the observed events for the decay  $D^0 \! \to \! K^- \, \pi^+$ , in Monte Carlo efficiencies due to statistics for detection of the decays  $D^0 \! \to \! K^- \, \pi^+$  and  $D^0 \! \to \! \overline{K}^0 \, \pi^+ \, \pi^-$ , due to varying the cuts on the  $K^0_s$  mass window, the range of the  $K^0_s$  sideband, the fit range, bin size and varying the background shape from 2 sd to 5 th order in the fit to the invariant masses of  $K^- \, \pi^+$ . These uncertainties are independent in the two decay modes. Some common systematic uncertainties due to tracking, particle identification, Monte Carlo simula-

tion and D productions are canceled. Monte Carlo study shows that the uncertainty in estimation of the double counting correction is about 3 %. The final systematic error is obtained by adding these uncertainties in quadrature, which yields a total systematic error of  $\pm 0.103$ .

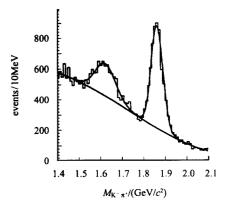


Fig. 4. Invariant mass distribution of  $K^-\pi^+$ .

Using the world averaged value of  $Br(D^0 \rightarrow K^-\pi^+)$ =  $(3.80 \pm 0.09)\%$ , we obtain the branching fraction for  $D^0 \rightarrow \overline{K}^0\pi^+\pi^-$  decay of

$$Br(D^0 \to \overline{K}{}^0\pi^+\pi^-) = (5.32 \pm 0.53 \pm 0.40) \%$$
, where the first error is statistical and the second systematic. The systematic uncertainty includes the systematic uncertainty in the ratio of the branching fractions for  $D^0 \to K_s^0\pi^+\pi^-$  and  $D^0 \to K^+\pi^-$ , and the uncertainty in the

## 4.1.2 The resonant substructure for $D^0 \rightarrow K_s^0 \pi^+ \pi^-$

branching fraction for the decay  $D^0 \rightarrow K^+ \pi^-$ .

A maximum likelihood fit to the Dalitz plot (Fig. 5(a)) is used to determine the decay branching fractions, relative phases into the modes  $K^{*-}\pi^{+}$ ,  $\overline{K}{}^{0}\,\rho^{0}$ , and three-body non-resonant. For each decay mode, we define a complex amplitude in the three-body phase space as:

$$A(D \rightarrow rc, r \rightarrow ab) = F_D F_r BW(r) M(abc|r)$$
, where the Blatt and Weisskopf form factors  $F_D$  and  $F_r$  take the forms as [10]. The relativistic Breit-Wigner propagator  $BW(r)$  as [11]:

$$\frac{-1}{m^2-m_0^2+\mathrm{i}\Gamma m_0},$$

where  $\Gamma$  is the energy dependent width, given by

$$\Gamma = \Gamma_0 \left( \frac{q}{q_0} \right)^{2J+1} \frac{m_0}{m} \frac{F_{\chi}^2(q^2)}{F_{\chi}^2(q_0^2)}.$$

The relevant value  $m_0$  and  $\Gamma_0$  are taken from Ref. [12]. The angular momentum part  $M(abc \mid r)$  are given in Helicity Formalism,

$$M(D \rightarrow rc) = \sum_{\lambda_r} D^0_{0\lambda_r} (-\phi_r, \theta_r, \phi_r) p^J_{ij} D^J_{\lambda_r^{r_0}} \times (-\phi_a, \theta_a, \phi_a) p^J_{a'} = (p_D p_a)^{J_r} d^J_{ij} (\theta_a),$$

with  $r \rightarrow ab$  and where, r is a resonant particle, a, b and c are pseudo-scalar mesons,  $p_{\rm D}$  and  $p_a$  is the momentum of D and a in r rest frame,  $J_r$  is the spin of particle r,  $\lambda_r$  is the helicity of particles r, and  $\theta_a$  is the helicity angle. The likelihood function L is defined as:

$$L = \prod_{\text{events}} \frac{R_{\text{S/B}}}{N_{F_{\text{S}}}} + \frac{F_{\text{B}}}{N_{F_{\text{B}}}},$$

where  $F_{\rm S}$  is the p.d.f. (probability density function) of signal. Since we can not determine the charm quantum number by  $K_{\rm s}^0$ , the data were fit to the average p.d.f. of  $D^0$  and  $\overline{D}^0$ . The  $F_{\rm S}$  contains a coherent sum of amplitudes,

$$A_{S}(D^{0}) = f_{1}e^{i\alpha_{1}} + A(K_{s}^{0}\pi^{-}\pi^{+}|K^{*-}) + f_{3}e^{i\alpha_{3}}A(\pi^{+}\pi^{-}K_{s}^{0}|\rho^{0}),$$

$$A_{S}(\overline{D}^{0}) = f_{1}e^{i\alpha_{1}} + A(K_{s}^{0}\pi^{+}\pi^{-}|K^{*+}) + f_{3}e^{i\alpha_{3}}A(\pi^{-}\pi^{+}K_{s}^{0}|\rho^{0}),$$

weighted by detector efficiency  $\epsilon$  and phase space.  $F_{\rm B}$  is the p.d.f. of background, containing a set of functions which model the K\*\*,  $\rho^0$  and non-resonant content of the events outside the signal region. The ratio of signal to background  $R_{\rm S/B}$  is a function of the invariant mass of the K $_{\rm s}^0\pi^+\pi^-$  combination, and is calculated for each event.  $N_{F_{\rm S}}$  and  $N_{F_{\rm B}}$  are the overall normalization of  $F_{\rm S}$  and  $F_{\rm B}$ , which are evaluated by using Monte Carlo techniques.

The events of  $K_s^0\pi^+\pi^-$  combinations with invariant masses within 1.5  $\sigma_{D^0}$  of  $D^0$  nominal mass were selected for the Dalitz plot analysis. Fig. 5. shows the Dalitz plot and the mass-squared projections for the decay  $D^0 \rightarrow K_s^0\pi^+\pi^-$ . In the Fig. 5(b)—(d) the 'cross' indicates the data, the higher histograms represent the values, and the lower histograms are the background component from the fit. To evaluate the p.d.f. of the background contribution, we defined two sidebands (low and high) as  $4\sigma < |M-M_D| < 7\sigma$ . For each entry, the momenta are recalculated using a kinematical fit according to the  $D^0$  mass.

The fit results are summarized in Table 1. In Table

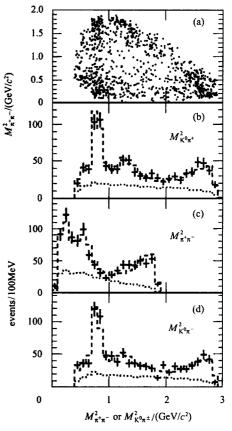


Fig. 5. Dalitz plot and mass-squared projections for the decay  $D^0 \rightarrow K_s^0 \pi^+ \pi^-$ . See text.

2, the decay branching fraction into a given mode is compared to the results from other experiments. The systematic errors are estimated by varying the events selection criteria, the method of background determination and the uncertainty of Monte Carlo efficiency. The largest source of systematic error comes from the parameterization of the background. To calculate systematic error due to the events selection, we change the window of the momentum cut, signal region definition and  $K_{\rm s}^0$  selection. The uncertainty of Monte Carlo efficiency is estimated to be 5 %. The systematic error due to the background is determined

Table 1. Fit result. Using the world average branching ratio  $Br(D^0 \to \overline{K}^0 \pi^+ \pi^-) = (5.92 \pm 0.35)\%^{[12]}$  we convert the fraction to branching ratio.

Decay Mode	relative fraction(%)	relative phase/(°)	branching ratio(%)
$K^* - \pi^+$ $(K^* - \rightarrow K^0 \pi^-)$	68.1 ± 3.6 ± 3.8	0(fixed)	6.05 ± 0.32 ± 0.49
$\overline{K}{}^{0}\rho^{0}$	19.8 ± 2.9 ± 1.8	- 138 ± 9	1.17 ± 0.17 ± 0.13
non- $K^{*-}\pi^{+}$ and non- $\overline{K}^{0}\rho^{0}$	22.7 ± 3.8 ± 2.5	- 114 ± 9	1.35 ± 0.22 ± 0.17

from a comparison of fits to the signal events using either backgrounds with a shape determined from the low sideband, the high sideband, the dalitz plot excluding the  $K^{\star}$  and  $\rho^0$  bands, or the varying the order of the background polynomial fit to the mass plot.

Table 2. Results from other experiments on the fraction and relative phase of the main contributions to  $D^0 \to \overline{K}{}^0 \, \pi^+ \, \pi^-$ .

D <sub>0</sub> →	ARGUS	MARK- III	BES- I
Κ* - π+	(71.8 ± 4.2 ± 3.0)%	(56 ± 4 ± 5)%	(68.1 ± 3.6 ± 3.8)%
	0°(fixed)	0°(fixed)	0°(fixed)
$\overline{\mathbf{K}}^{0}  \rho^{0}$	(22.7 ± 3.2 ± 0.9)%	$(12 \pm 1 \pm 7)\%$	$(19.8 \pm 2.9 \pm 1.8)\%$
	(-137 ± 7)°	$(90 \pm 30)^{\circ}$	$(-138 \pm 9)^{\circ}$
non-K * - $\pi$ + and non- $\overline{K}^0 \rho^0$	_	(33 ± 5 ± 10)% incoherent	$(22.7 \pm 3.8 \pm 2.5)\%$ $(-114 \pm 9)^{\circ}$

## 4.2 The decay $D^0 \rightarrow \overline{K}^0 K^+ K^-$

## 4.2.1 The branching fraction for $D^0 \rightarrow \overline{K}^0 K^+ K^-$

The analysis of  $D^0 \rightarrow K_s^0 \, K^+ \, K^-$  is similar to that of  $D^0 \rightarrow K_s^0 \, \pi^+ \, \pi^-$  with the substitution of Kaons for the non- $K_s^0$  pions. Fig. 6. shows the distribution of the invariant masses of  $K_s^0 \, K^+ \, K^-$  combinations. Fitting to the mass spectrum with a Gaussian function representing the  $D^0$  signal and a second order polynomial describing the background gives signal of  $34.3 \pm 8.1$  events for  $D^0 \rightarrow K_s^0 \, K^+ \, K^-$  decay after correcting to doubly counted events and subtracting the non-resonant ( $D^0 \rightarrow (\pi^+ \, \pi^-)_{non-K_s^0} \, K^+ \, K^-$ ) background. A Monte Carlo study gives the detection efficiency of  $\epsilon_{D^0 \rightarrow \overline{K}^0 \, K^+ \, K^-}^{MC} = 0.0140 \pm 0.0008$ , where the error is statistical.

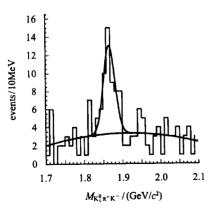


Fig.6. Invariant mass distribution of K<sub>s</sub><sup>0</sup> K<sup>+</sup> K<sup>-</sup>.

Using the numbers of the observed events for the decays  $D^0\!\to\! K^0_s\,K^+\,K^-$ ,  $D^0\!\to\! \overline K^0\,\pi^+\,\pi^-$  and the relative de-

tection efficiencies, the ratio of branching fractions for  $D^0 \to \overline{K}^0 \, K^+ \, K^-$  and  $D^0 \to \overline{K}^0 \, \pi^+ \, \pi^-$ 

$$\frac{Br(D^{0} \to \overline{K}^{0}K^{+}K^{-})}{Br(D^{0} \to \overline{K}^{0}\pi^{+}\pi^{-})} = 0.175 \pm 0.041 \pm 0.024$$

is obtained, where the first error is statistical and the second systematic. The systematic error is estimated based on the changes in the ratio due to the uncertainties in the number of the observed events for the decay  $D^0 \! \to \! \overline{K}^0 \pi^+ \pi^-$ , in the Monte Carlo efficiencies for detection of the decays  $D^0 \! \to \! \overline{K}^0 \pi^+ \pi^-$ ,  $D^0 \! \to \! \overline{K}^0 K^+ K^-$  and the uncertainties in doubly counted corrections.

Using the world averaged branching fraction for  $D^0 \longrightarrow K^0_*\pi^+\pi^-$ , we obtain

 $B(D^0 \to \overline{K}^0 K^+ K^-) = (1.04 \pm 0.24 \pm 0.16) \%$ , where the first error is statistical and the second systematic. The systematic error includes the systematic uncertainty in the ratio of branching fractions for  $D^0 \to \overline{K}^0 K^+ K^-$  and  $D^0 \to \overline{K}^0 \pi^+ \pi^-$ , and the uncertainty in the branching fraction for  $D^0 \to K_s^0 \pi^+ \pi^-$ .

## 4.2.2 The branching fraction for $D^0 \rightarrow \overline{K}^0 \phi$

The \$\phi\$ mesons are reconstructed in its decay to K+K- and selected by using the event selection criteria described in Section 3. In this measurement the region  $1.0044 < m_{K^+K^-} < 1.0344 \text{ GeV}/c^2$  is defined as the  $\phi$ signal region, and the intervals 0.98-1.00 GeV and 1.05-1.2 GeV are considered as background regions for the  $\varphi$  . We then compute  $\varphi$  and  $K^0_s$  invariant mass . To enhance the  $D^0 \rightarrow \phi K_s^0$  candidates a cut on the helicity angle,  $\theta_K^+$  of the  $K^+$  is required to the  $K_s^0\varphi$  candidates; we require  $|\cos\theta_{\kappa^+}| > 0.3$ . The resulting invariant mass of the  $K_s^0 \phi$  spectrum is shown in Fig. 7. The  $K_s^0 \phi$  mass regions from 1.8348 to 1.8948 GeV within the  $\pm 2\sigma_{m_n0}$ mass region is defined as Do signal region, and the regions from 1.7 to 2.1  $\text{GeV}/c^2$  excluding the region from 1.81 to 1.91 GeV are defined as sideband background control regions for the D0 meson. As shown in the Fig.7, 17 events are found as  $D^0 \rightarrow \overline{K}{}^0 \phi$  candidates, and 6 events are selected as  $D^0 \rightarrow \overline{K}^0 \phi$  side band events. Using the  $D^0$ side band events, a total of  $1.2 \pm 0.5$  events has been estimated as the background among the  $\ensuremath{D^0}$  candidates. In the Fig.7. the shaded histogram shows the distribution of the invariant masses of  $K^0_s K^+ K^-$  combinations by means of requiring the invariant mass of  $K^+K^-$  to be within the  $\varphi$  side bands, and requiring that the number of events in each bin is normalized to evaluate the number of background in the  $\varphi$  signal interval of  $\pm$  15 MeV/ $c^2$ . Using the  $\varphi$  side band events, a total of  $0.8 \pm 0.6$  events has been estimated as the  $D^0 \to \overline{K}^0$  ( $K^+K^-$ )<sub>non- $\varphi$ </sub> background among the  $D^0$  candidates. Subtracting the background contributions to both the  $D^0$  and the  $\varphi$  and subtracting 1 event due to double counting, we obtain  $14.0 \pm 4.3 \ D^0 \to \overline{K}^0 \varphi$  events.

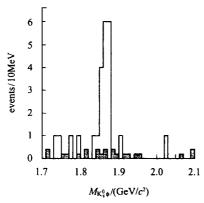


Fig. 7. Invariant mass distribution of  $K_s^0 \phi$ .

A Monte Carlo simulation of the decay  $D^0 \to \overline{K}{}^0 \varphi$  is used to determine the detection efficiency . This yields the efficiency of  $\varepsilon^{MC}_{D^0 \to \overline{K}{}^0 \varphi} = (\, 0 \, . \, 0053 \, \pm \, 0 \, . \, 0003 \, )$  . The ratio of branching fractions for  $D^0 \to \overline{K}{}^0 \varphi$  and  $D^0 \to \overline{K}{}^0 \pi^+ \, \pi^-$  is given by

$$\frac{Br(D^0 \to \overline{K}^0 \phi)}{Br(D^0 \to \overline{K}^0 \pi^+ \pi^-)} = 0.189 \pm 0.058 \pm 0.022,$$

where the first error is statistical and the second systematic. The systematic error arises from the uncertainties in the numbers of the observed events for the decay  $D^0 \rightarrow \overline{K}{}^0\pi^+\pi^-$ , in the Monte Carlo efficiencies for detection of the decays  $D^0 \rightarrow \overline{K}{}^0\pi^+\pi^-$  and  $D^0 \rightarrow \overline{K}{}^0\varphi$ , and the uncertainties due to varying the helicity angle  $\theta_K$  and the  $\varphi$  mass cuts.

$$Br(D^0 \to \overline{K}^0 \phi) = (1.12 \pm 0.34 \pm 0.15) \%$$

where the first error is statistical and the second systematic, which results from the uncertainty in the ratio of branching fractions for  $D^0\!\to\!\overline K^0\,\varphi$  and  $D^0\!\to\!\overline K^0\,\pi^+\,\pi^-$ , and the uncertainty in the branching fractions for  $D^0\!\to\!\overline K^0\,\pi^+\,\pi^-$ .

## 4.2.3 The branching fraction for $D^0 \rightarrow \overline{K}^0 (K^+ K^-)_{nor-\Phi}$

In order to estimate the decay branching fraction of  $D^0 \to \overline{K}^0$  ( $K^+ K^-$ )<sub>non- $\phi$ </sub> we require the invariant mass of the  $K^+ K^-$  outside of the  $\phi$  mass region  $|M_{K^+K^-} - M_{\phi}| > 0.022 \text{GeV}/c^2$ . Fig. 8. shows the  $K_s^0$  ( $K^+ K^-$ )<sub>non- $\phi$ </sub> invariant mass distribution. Using a Gaussian signal function plus a second order polynomial background to fit this mass spectrum with correcting to the doubly counted events and subtracting the number of background events  $0.0_{-0.00}^{+0.05}$  for the decay  $D^0 \to K^+ K^- (\pi^+ \pi^-)_{\text{non-}K^0}$ , we obtain the signal of  $12.5 \pm 6.2$  events. A corresponding Monte Carlo efficiency for detection of this decay is  $0.0200 \pm 0.0010$ . Based on the  $12.5 \pm 6.2$   $D^0 \to \overline{K}^0$  ( $K^+ K^-$ )<sub>non- $\phi$ </sub> events, the ratio of the branching fractions for  $D^0 \to \overline{K}^0$  ( $K^+ K^-$ )<sub>non- $\phi$ </sub> over  $D^0 \to \overline{K}^0 \pi^+ \pi^-$ 

$$\frac{Br(D^0 \to \overline{K}^0 K^+ K^-_{non-\phi})}{Br(D^0 \to \overline{K}^0 \pi^+ \pi^-)} = 0.045 \pm 0.022 \pm 0.004$$

is obtained, where the first error is statistical and the second systematic. The systematic error is estimated based on the changes of the ratio due to the uncertainties in the number of the observed events for the decay  $D^0 \rightarrow \overline{K}^0\pi^+\pi^-$ , in the Monte Carlo efficiencies for detection of the decays  $D^0 \rightarrow \overline{K}^0\pi^+\pi^-$  and  $D^0 \rightarrow \overline{K}^0(K^+K^-)_{non.\phi}$ , and the double counting corrections for the decays  $D^0 \rightarrow \overline{K}^0\pi^+\pi^-$  and  $D^0 \rightarrow \overline{K}^0(K^+K^-)_{non.\phi}$ . The combined effect of these sources is obtained by adding in the uncertainties in quadrature, which yields a total systematic error of  $\pm 0.004$ .

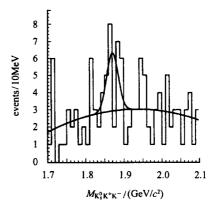


Fig. 8. Invariant mass distribution of  $\overline{K}^0\,(\,K^+\,\,K^-\,)_{\text{non-$^{\circ}$}}\,.$ 

Using the world average decay branching fraction for  $D^0\!\to\!\overline K^0\pi^+\pi^-$ , we obtain the decay branching fraction of

 $Br(D^0 \to \overline{K}^0(K^+ K^-)_{non-\phi}) = (0.27 \pm 0.13 \pm 0.03) \%$ . The second error is systematic, reflecting the systematic uncertainty in the ratio of branching fractions for  $D^0 \to \overline{K}^0(K^+ K^-)_{non-\phi}$  and  $D^0 \to \overline{K}^0\pi^+\pi^-$ , and the uncertainty in the branching fraction for  $D^0 \to K_s^0\pi^+\pi^-$ .

#### 5 Conclusion

In summary, using the data collected with BES- I detector at BEPC Collider we have measured the branching fraction for  $D^0 \rightarrow \overline{K}{}^0\pi^+\pi^-$  to be  $(5.37 \pm 0.52 \pm 0.40)\%$ . Using a coherent amplitude analysis we measured the branching fractions for the decays  $D^0 \rightarrow K^* - \pi^+$ ,  $D^0 \rightarrow \overline{K}{}^0\rho^0$  and  $D^0 \rightarrow \overline{K}{}^0\pi^+\pi^-_{\text{non-resonant}}$  to be  $(6.05 \pm 0.32 \pm 0.49)\%$ ,  $(1.17 \pm 0.17 \pm 0.13)\%$  and

 $(1.35 \pm 0.22 \pm 0.17)\%$ , respectively. We have measured the branching fractions  $Br(D^0 \rightarrow f)$  to be  $(1.04 \pm 0.24 \pm 0.16)\%$  for  $f = \overline{K}^0 K^+ K^-$ ,  $(1.12 \pm 0.34 \pm 0.15)\%$  for  $f = \overline{K}^0 \phi$ , and  $(0.27 \pm 0.13 \pm 0.03)\%$  for  $f = \overline{K}^0 (K^+ K^-)_{non-\phi}$ .

Our results are consistent with those from ARGUS<sup>[5]</sup>, MARK- $\prod$ <sup>[6]</sup>, CLEO<sup>[7]</sup> and E687<sup>[8]</sup> measurements. Our measured value of branching fraction  $Br(D^0 \to \overline{K}^0 \phi) = (1.12 \pm 0.34 \pm 0.15)\%$  is also consistent within the error with the Enhancement W-exchange model<sup>[13]</sup> and some other models<sup>[14]</sup> predictions.

The BES collaboration thanks the BEPC staff for their strong efforts and thanks the member of the IHEP computing center for their helpful assistance.

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## 遍举衰变过程 $\mathbf{D}^0 \rightarrow \mathbf{K}_s^0 \pi^+ \pi^- \mathbf{A} \mathbf{D}^0 \rightarrow \mathbf{K}_s^0 \mathbf{K}^+ \mathbf{K}^-$ 及其共振态结构的实验研究 \*

## BES 合作组

白景芝 卞建国 蔡啸 班勇5 常劲帆 陈和生 陈宏芳1 陈江川 陈杰8 陈元柏 迟少鹏 初元萍 崔象宗 戴又善3 戴玉梅12 董燎原 杜书先10 杜志珍 方建 房双世 傅成栋 富洪玉 符力平11 高翠山 高美丽 高原宁14 宫鸣宇 龚文煊 顾树棣 过雅南 郭义庆 郭子金'韩世温 何炬 何康林 何瑁2 贺翔 衡月昆 洪涛 胡海明 胡涛 黄光顺 黄亮" 黄秀萍 季晓斌 姜春华 江晓山 金大鹏 金山 金艳 柯尊建 赖元芬 李飞 李刚 李会红6 李家才 李金 李侃" 李秋菊 李仁英 李如柏 李蔚 李卫国 李学潜8 李雪松14 刘朝峰10 刘春秀 刘芳1 刘峰6 刘怀民 刘建北 刘觉平10 刘荣光 刘延 刘振安 刘钟秀 鲁公儒9 吕志坚 罗小兰 马恩成 马凤才12 吕峰 吕海江 吕军光 马基茂 莫晓虎7 聂晶 毛泽普 孟祥承 聂振东 彭海平1 漆纳丁 钱诚德4 邱进发 荣 刚 <sup>1)</sup> 沈定力 沈红 沈肖雁 盛华义 石峰 宋立温 孙汉生 孙胜森! 孙永昭 孙志嘉 唐素秋 唐晓 田丁 田雨润14 童国梁 王近珠 王君 王佩良 王平 王文峰 王岚 王灵淑 王曼 王萌 王贻芳 王 喆 王征 王峥 王至勇 魏诚林 吴宁 夏小米 谢小希 许国发 徐晔 薛生田 阎沐霖! 鄢文标 杨贵安 杨洪勋14 杨杰1 杨胜东 叶铭汉7 叶云秀1 应军5 于传松 俞国威 苑长征 袁建明 袁野 岳骞 臧石磊 曾云11 张丙新 张炳云 张长春 张达华 张家文 张建 张军梅9 张良生 张勤俭 张少强 张学尧2 张一云13 张勇军5 张月元 张子平1 章红宇 赵棣新 赵家伟! 赵京伟 赵平平

<sup>2003 - 02 - 25</sup> 收稿, 2003 - 09 - 11 收修改稿

<sup>\*</sup>国家自然科学基金(19991480),国家杰出青年科学基金(10225524,10225525),中国科学院九五重大及特别支持项目(KJ95T - 03),中国科学院百人计划基金(U - 24,U - 25),中国科学院知识创新基金(U - 602,U - 34)资助

<sup>1)</sup> E-mail:rongg@mail.ihep.ac.cn

赵维仁 赵豫斌 赵政国<sup>1)</sup> 郑建平 郑林生 郑志鹏 钟学初周宝庆 周高明 周莉 周能峰 朱科军 朱启明 朱莹春朱永生 朱自安 祝玉灿 庄保安 邹冰松

(中国科学院高能物理研究所 北京 100039) 1(中国科学技术大学近代物理系 合肥 230027)

2 (山东大学物理系 济南 250100)

3 (浙江大学物理系 杭州 310028)

4(上海交通大学应用物理系 上海 200030)

5(北京大学技术物理系 北京 100871)

6 (华中师范大学粒子物理研究所 武汉 430079)

7 (中国高等科学技术中心 北京 100080)

8 (南开大学物理学院 天津 300071)

9 (河南师范大学物理与信息工程学院 新乡 453002)

10 (武汉大学物理与电子信息学院 武汉 430072)

11 (湖南大学应用物理系 长沙 410082)

12 (辽宁大学物理系 沈阳 110036)

13 (四川大学物理系 成都 610064)

14 (清华大学物理系 北京 100084)

摘要 利用北京谱仪(BES-I)在北京正负电子对撞机(BEPC)e<sup>+</sup>e<sup>-</sup>质心系能量为 4.03GeV 处采集的积分 亮度为 22.3pb<sup>-1</sup>的数据,研究了 $D^0 \to K^0_s \pi^+ \pi^-$ , $D^0 \to K^0_s K^+ K^-$ 的衰变及其末态的共振结构.实验测得 $D^0 \to K^0_s \pi^+ \pi^-$  过程的分支比为(5.32±0.53±0.40)%; $D^0 \to K^* - \pi^+$ , $D^0 \to \overline{K}^0 \rho^0 \pi D^0 \to K^0_s (\pi^+ \pi^-)_{non-resonance}$  过程的分支比分别为(6.05±0.32±0.49)%,(1.17±0.17±0.13)% 和(1.35±0.22±0.17)%;测得 $D^0 \to K^0_s K^+ K^-$ , $D^0 \to \overline{K}^0 \phi \pi D^0 \to \overline{K}^0 (K^+ K^-)_{non-4}$ 的分支比分别为(1.04±0.24±0.16)%,(1.12±0.34±0.15)% 和(0.27±0.13±0.03)%.

关键词 北京谱仪 北京正负电子对撞机 D介子 分支比

<sup>1)</sup> University of Michigan, Ann Arbor, MI 48109, USA